

# MICROSPEAKERS – HYBRIDS BETWEEN HEADPHONES AND LOUDSPEAKERS

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*Klippel, Microspeaker – Hybrids between loudspeakers and headphones ..., 1*



## Content

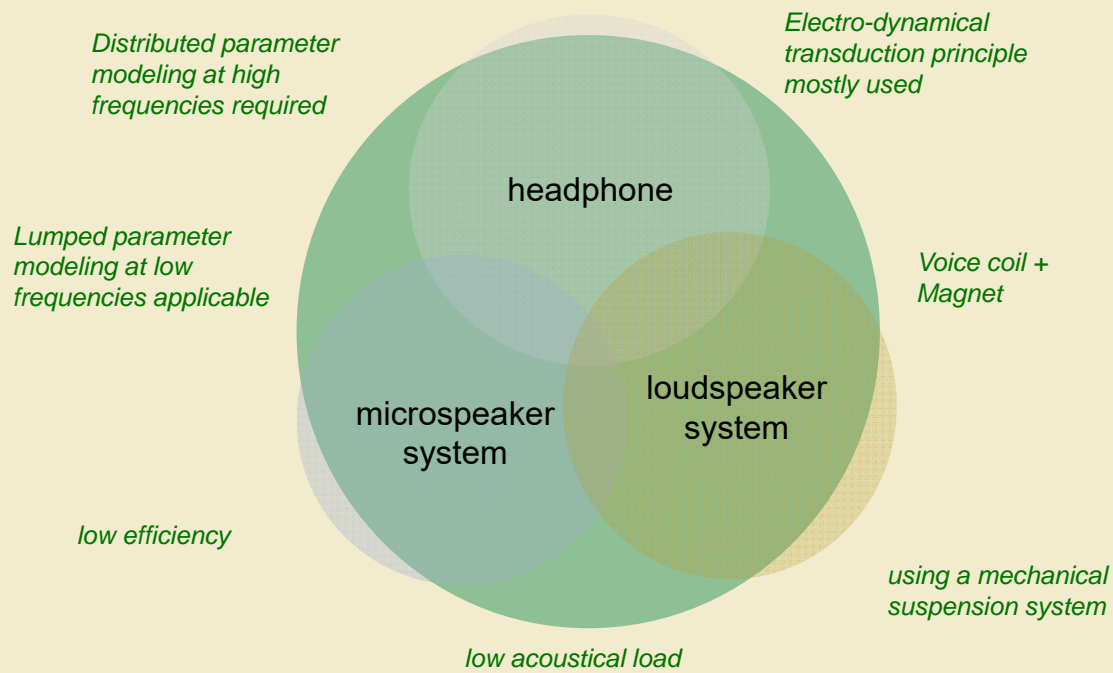
1. Motivation
  - similarities and particularities
2. Basic Transducer Modeling
  - linear, time-invariant, lumped parameter
3. Progress in Transducer Modeling
  - higher-order system function,
  - modal vibration
  - radiation into 3D space
  - nonlinear, time variant
4. Consequences for Transducer Design

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# Similarities

between headphones, microspeakers and loudspeakers

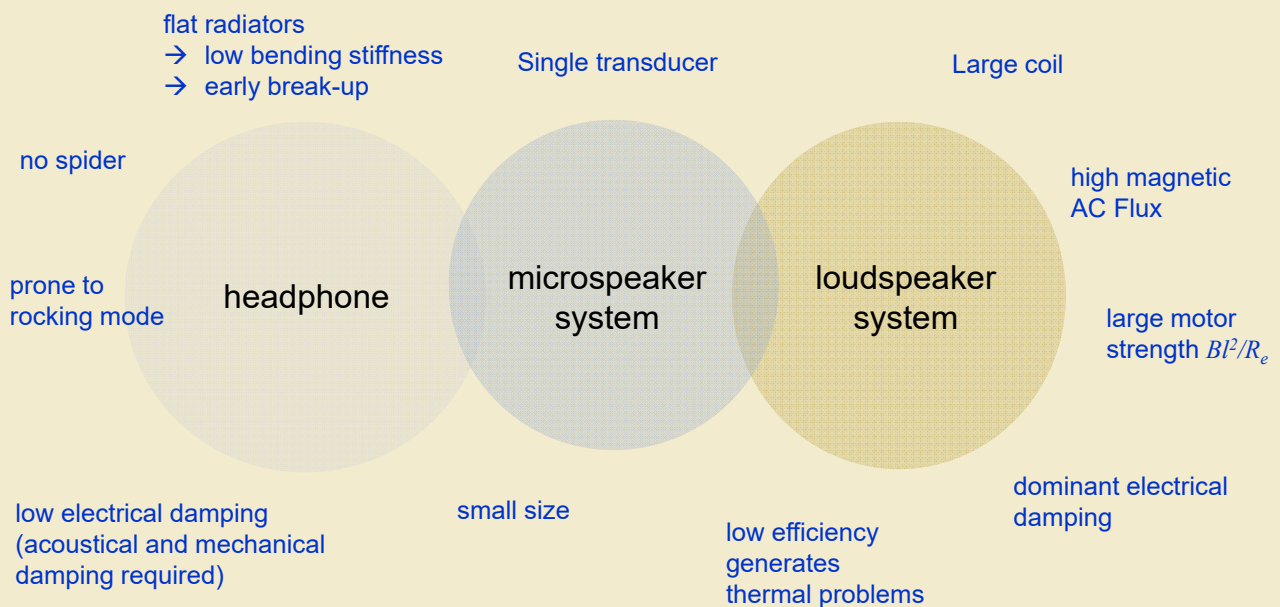


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# Particularities

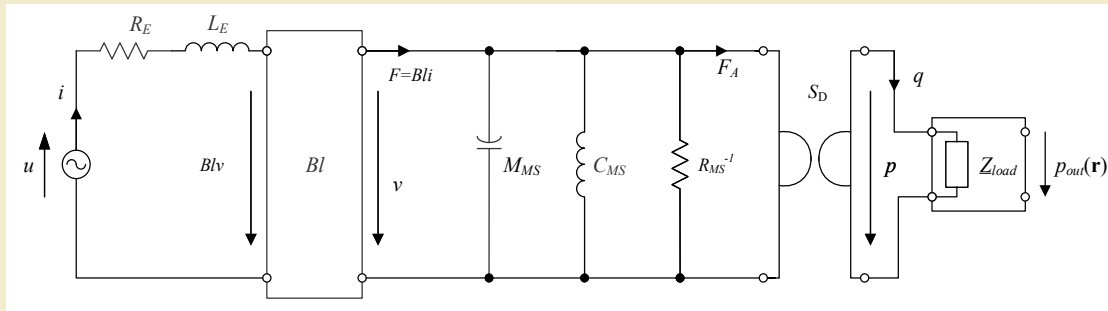
between headphones, microspeakers and loudspeakers



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# Basic Electroacoustical Modeling



## Assumptions:

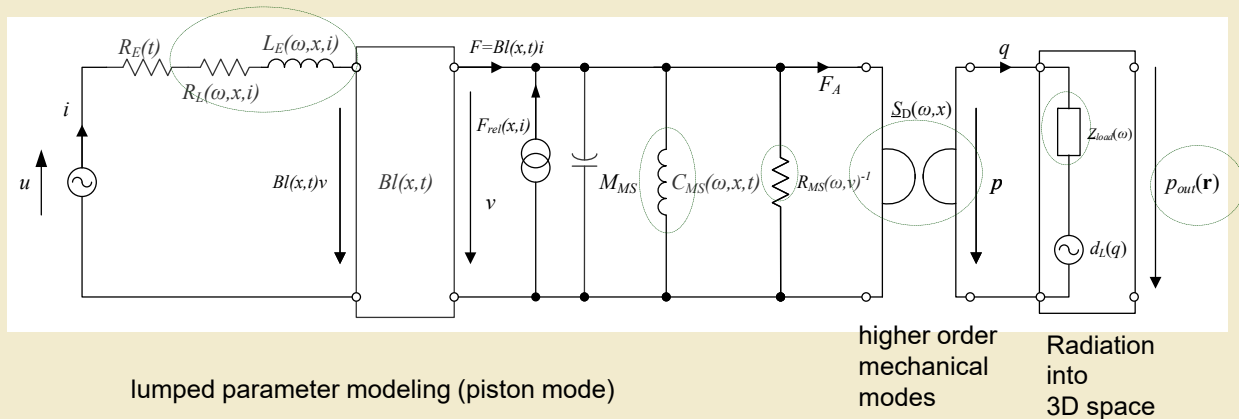
- no heating of the voice coil ( $\rightarrow R_E = \text{const.}$ )
- eddy currents neglected (loss-less inductance  $\rightarrow L_E$ )
- nonlinearities neglected (e.g.  $Bl = \text{const.}$ )
- visco-elasticity neglected ( $\rightarrow C_{MS} = \text{const.}$ )
- simplified damping model (viscously damped system  $\rightarrow C_{MS}$ )
- higher-order modes neglected (piston mode described by  $S_D$ )

$\rightarrow$  linear, time invariant, single input based on lumped parameter modeling

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# Extended Electroacoustical Modeling



## Higher-order linear transfer function

- Lossy inductance
- visco elastic creep modeling
- Modal vibration, radiation

Nonlinearities

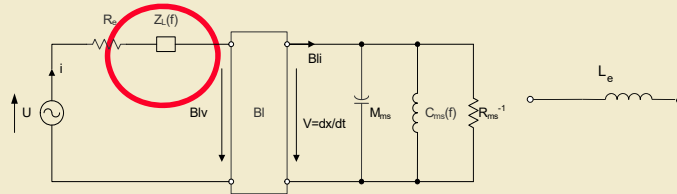
Time variant properties

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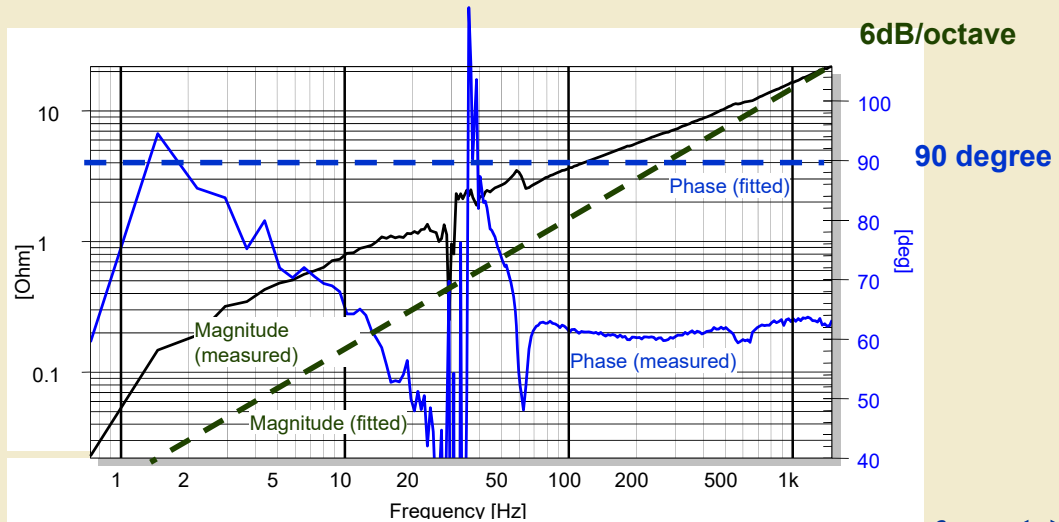


# Lossy Inductance $Z_L(j\omega)$

measured curves fitted by an ideal inductance



- 1 Parameter only
- Large deviation
- limited use



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# Mechanical Compliance $C_{md}(f)$

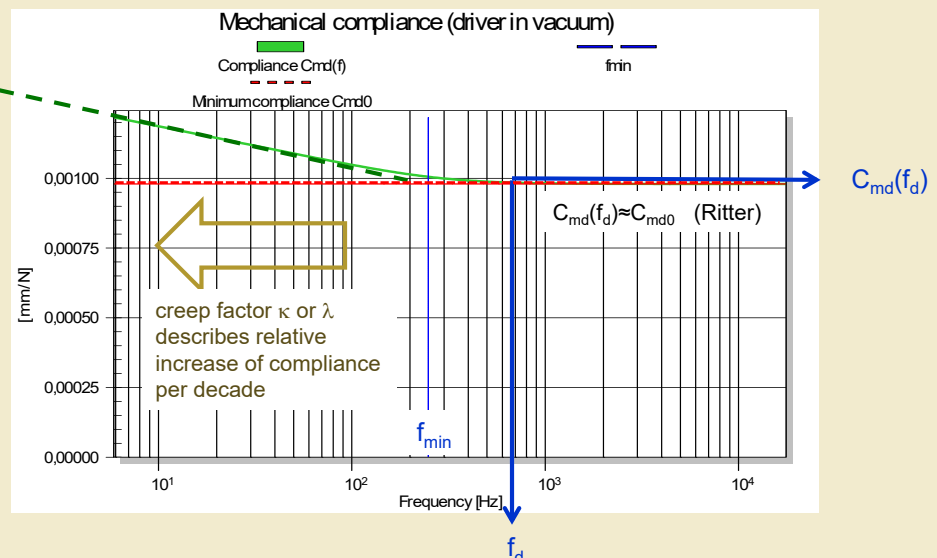
$$C_{MD}(f) = C_{min} \left( 1 - \kappa \log_{10} \left( \frac{(f/f_{min})}{\sqrt{1 + (f/f_{min})^2}} \right) \right)$$

creep factor  $\kappa$  or  $\lambda$

**EFFECT:**  
compliance  
increases to lower  
frequencies

**CAUSE:**  
viscoelasticity of  
the material

**CONSEQUENCES:**  
more displacement  
than predicted by  
traditional modeling



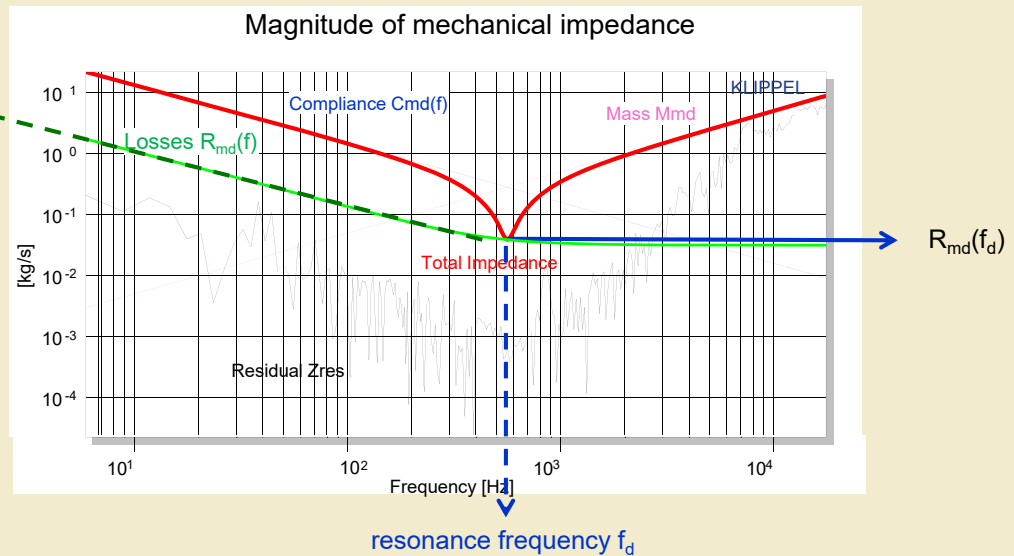
# Mechanical Resistance $R_{md}(f)$

$$R_{MD}(f) = R_0 - \kappa C_{min} \log_{10}(e) \left( \frac{\pi}{2} - \tan^{-1} \left( \frac{f}{f_{min}} \right) \right)$$

**EFFECT:**  
losses increases to lower frequencies

**CAUSE:**  
viscoelasticity transfers compliance into losses

**CONSEQUENCE:**  
electrical impedance increased below resonance (not critical)

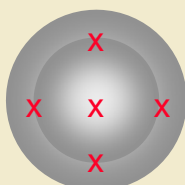
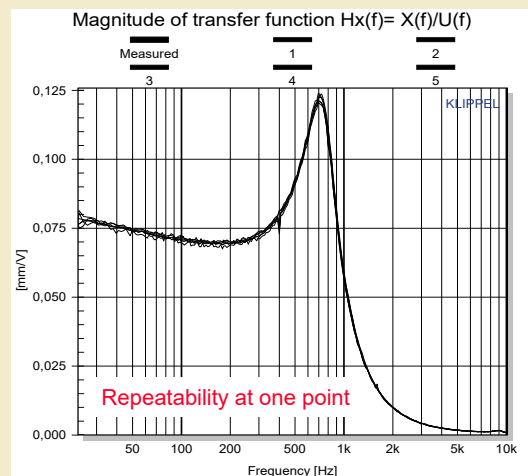
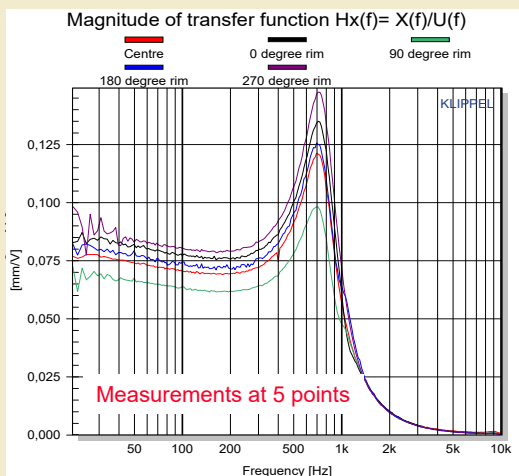


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## Voice Coil Displacement

Laser measurement on Microspeakers and Headphones



**Conclusion:**

- No piston mode
- Spatial averaging is required

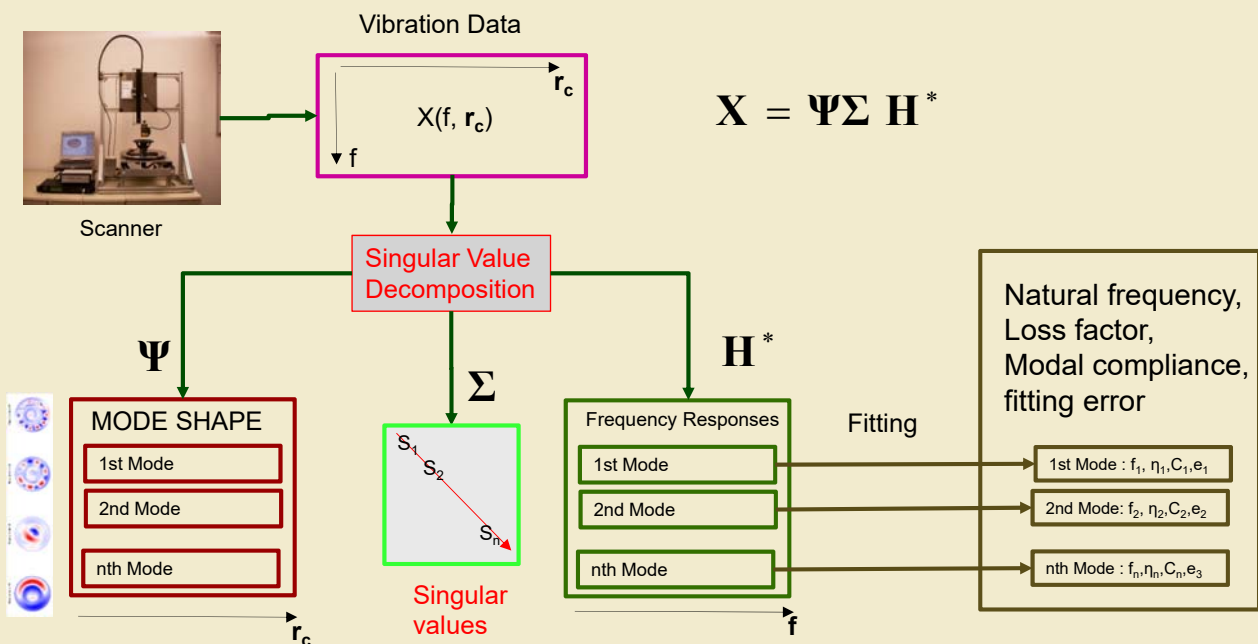
$$\underline{x}_{coil}(\omega) = \frac{\int_0^{2\pi} \underline{x}(\omega, r_{avg}, \varphi) d\varphi}{2\pi}$$

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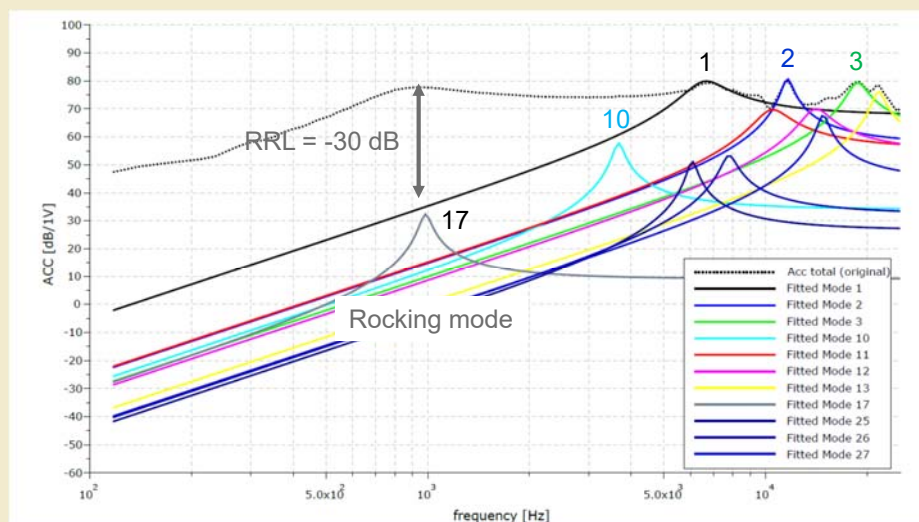
# Experimental Modal Analysis

not restricted to round radiators

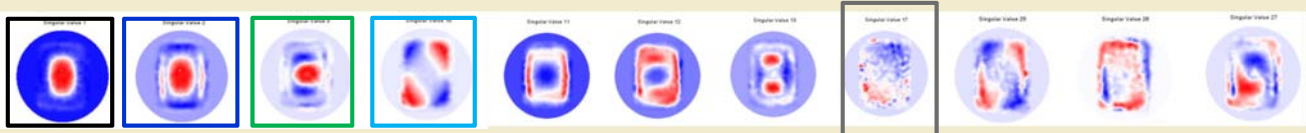


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## Modalanalysis of a Microspeaker

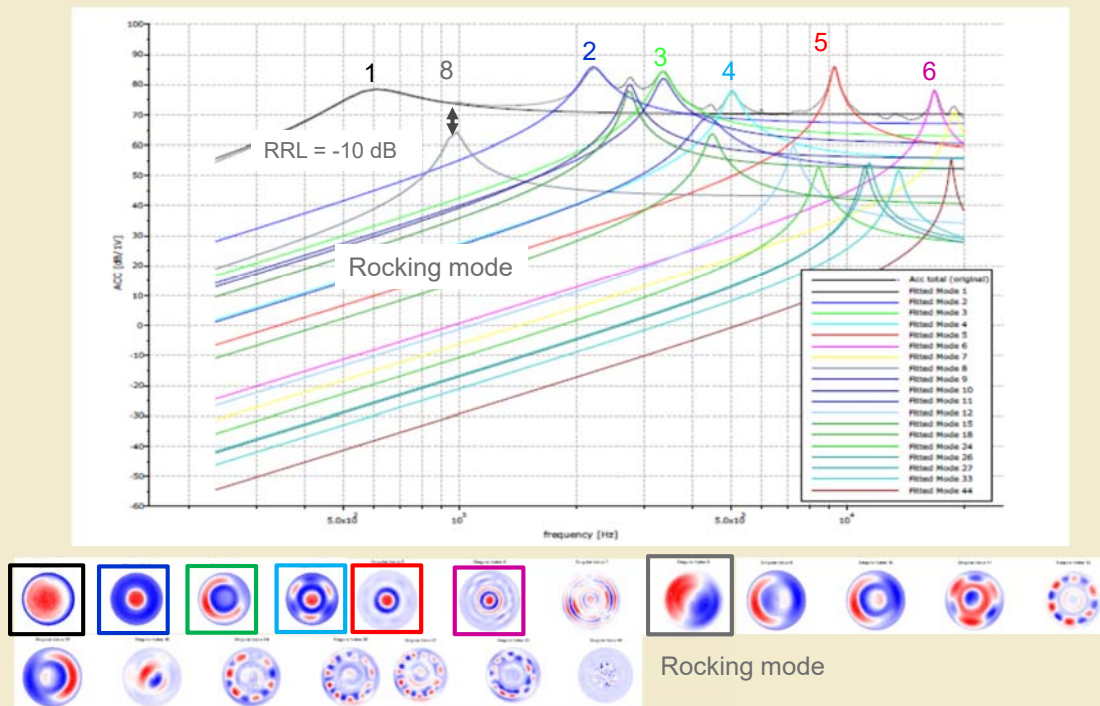


Rocking mode



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# Modalanalysis of a Headphone



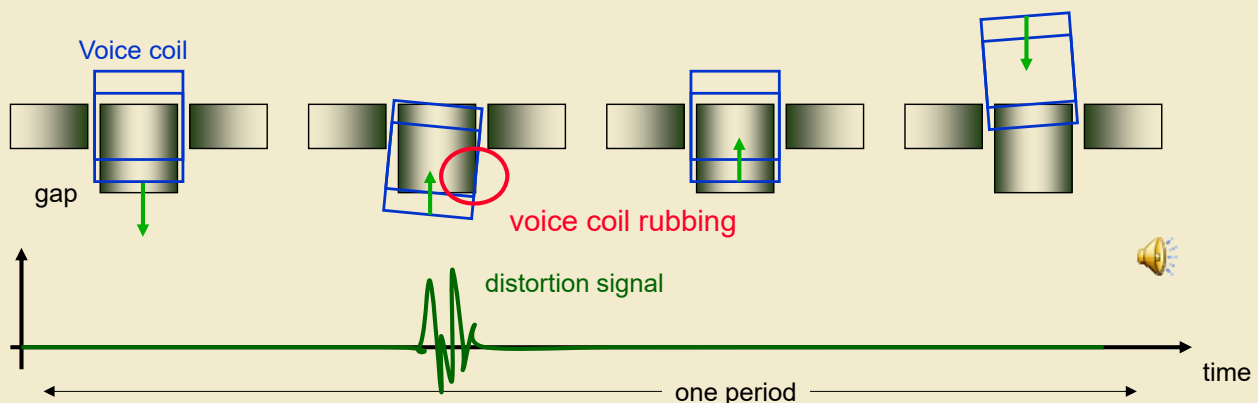
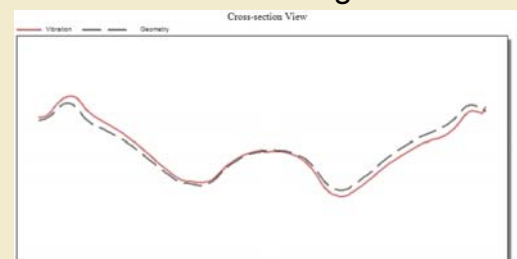
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## Loudspeaker Defect: Voice Coil Rubbing

- signal contains reproducible and stochastic components

Cause: rocking mode at 328 Hz

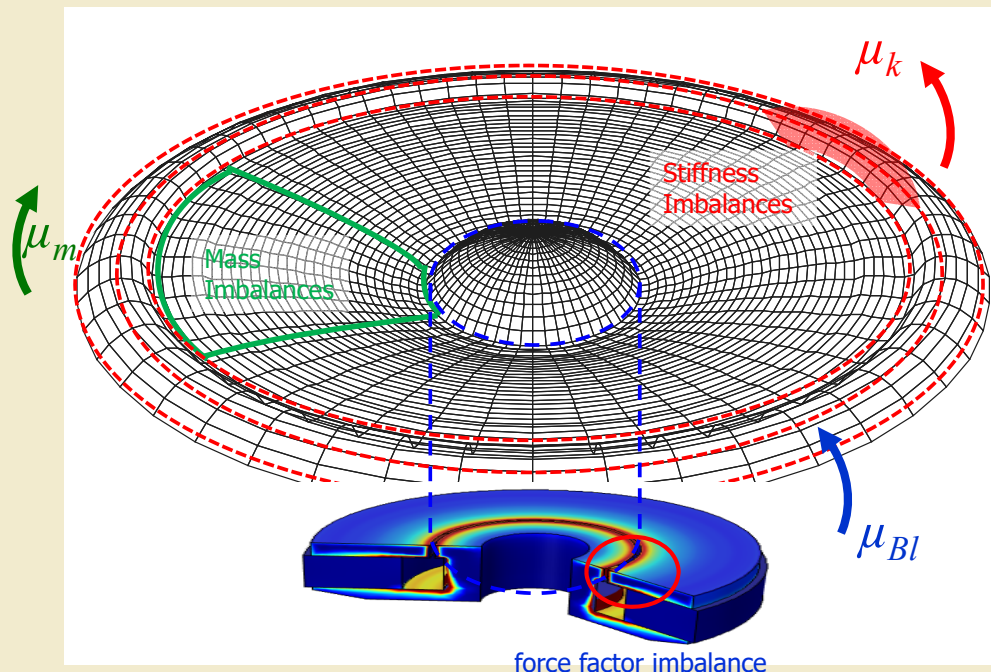


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# What Causes Rocking Modes ?

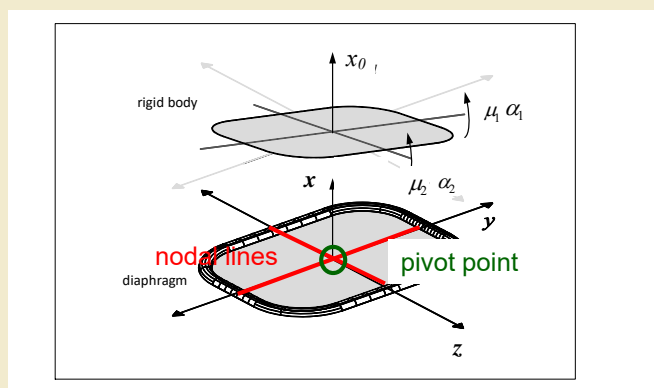


Which root cause excites the rocking ? → mass, stiffness, force factor  
 Where is the root cause located ? → angle showing the direction  
 How to assess the magnitude of the excitation ? → moments

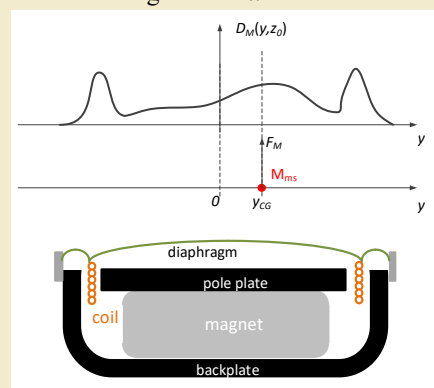
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## Mass Imbalance



mass distribution function  $D_m(y, z)$  of the moving mass in  $x$  direction



If the center of gravity is not at the pivot point ( $y_{CG} \neq 0, z_{CG} \neq 0$ ) the translational displacement  $x_0$  and the tilting angles  $\tau_1$  and  $\tau_2$  will generate the moments exciting the rocking modes

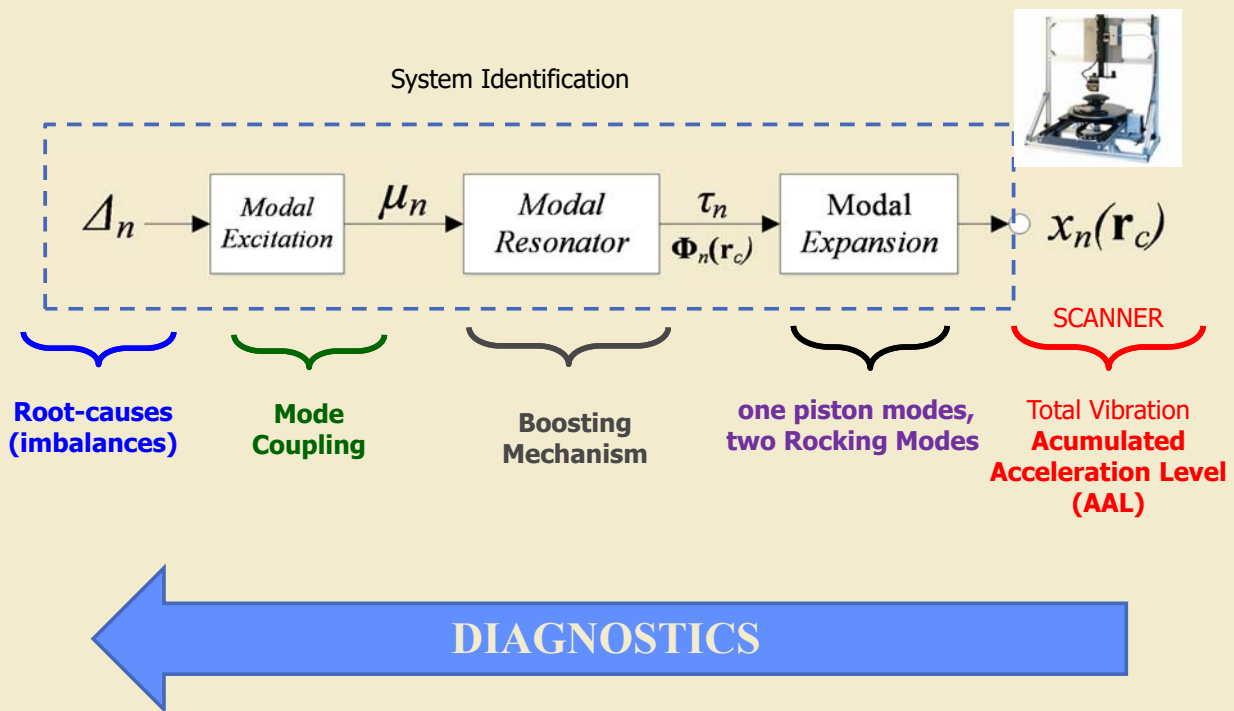
Imbalances (mass, stiffness, BI) → Moments  $\mu_1 \mu_2$  → Tilting angles  $\alpha_1 \alpha_2$

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# A New Measurement Technique

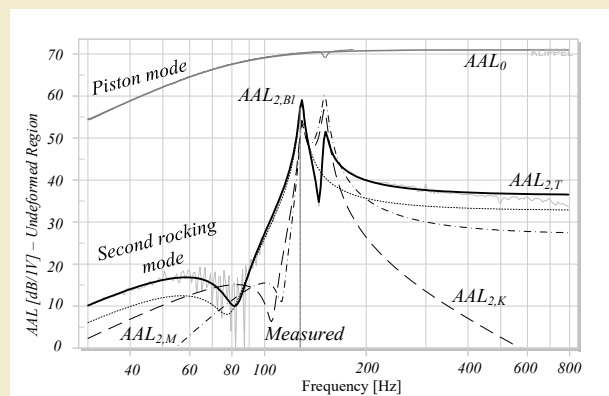
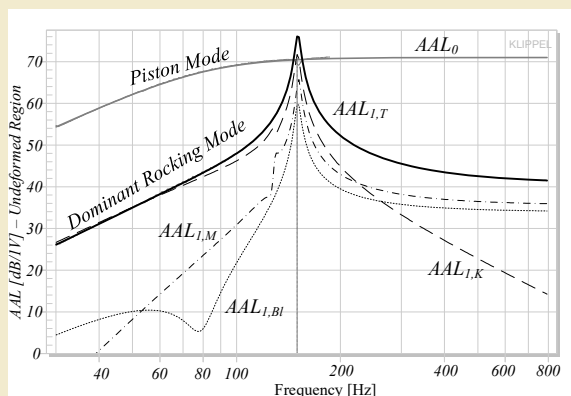


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## Application in Transducer Diagnostics (1)

Example Headphone transducer



Relative Rocking Level RRL(dB)	Dominant (n=1)	Second (n=2)
Total contribution (T)	RRL <sub>1,T</sub> = 5.4	RRL <sub>2,T</sub> = -12.9
Mass Imbalance (M)	RRL <sub>1,M</sub> = -8.6	RRL <sub>2,M</sub> = -18.4
Stiffness Imbalance (K)	RRL <sub>1,K</sub> = 1.4	RRL <sub>2,K</sub> = -17.7
Force factor Imbalance (BI)	RRL <sub>1,BI</sub> = -9.6	RRL <sub>2,BI</sub> = -12.6

### Conclusions:

- Good agreement between measurement and modelling
- First rocking mode has significant amplitude (more energy than piston mode)
- Stiffness imbalance provides the largest contribution (dominant cause)

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# Application in Transducer Diagnostics (3)

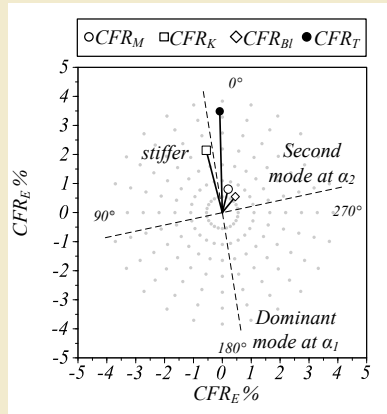
## Example Headphone transducer

### Root Cause of the Rocking Mode (Imbalance)

Center of	Coordinates	Value
Gravity (M)	$d_M$	0.08 mm
	$\gamma_M$	168°
Stiffness (K)	$d_K$	0.73 mm
	$\gamma_K$	17.54°
Force factor (BI)	$d_{BI}$	0.9 mm
	$\gamma_{BI}$	320°

### Excitation of the Rocking Resonator

Imbalance	Characteristics	Value
Mass (M)	$CFR_M$	0.83 %
	$\beta_M$	345.9°
Stiffness (K)	$CFR_K$	2.22 %
	$\beta_K$	14.6°
Force factor (BI)	$CFR_{BI}$	0.71 %
	$\beta_{BI}$	320.8°
Total (M,K,BI)	$CFR_T$	3.49%
	$\beta_T$	1.5°



### Conclusions:

- A small stiffness imbalance (0.73 mm offset from pivot point) is the root cause
- High Quality factor (> 30) of the modal rocking resonator generates high amplitudes at resonance (150 Hz)

Modal resonator (n=1,2)	First mode (n=1)	Second mode (n=2)
Resonance frequency	$f_1 = 151 \text{ Hz}$	$f_2 = 129 \text{ Hz}$
Relative gain at $f_n$	$RG_1 = 36 \text{ dB}$	$RG_2 = 31.6 \text{ dB}$
Loss factor	$\eta_1 = 0.016$	$\eta_2 = 0.014$
Quality factor	$Q_1 = 30.2$	$Q_2 = 34.7$

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## Effective Radiation Area $S_D$

### Definition

Radiator's surface

replaced by

Rigid piston

$$\underline{S}_D(\omega) = \frac{\int_{S_c} \underline{v}(\omega, \mathbf{r}_c) dS_c}{\underline{v}_{coil}(\omega)}$$

using mean voice coil velocity

$$\underline{v}_{coil}(\omega) = \frac{\int_0^{2\pi} \underline{v}(\omega, r_{coil}, \varphi) d\varphi}{2\pi}$$

$S_D = |\underline{S}_D(\omega_0)|$

Reading the absolute value at fundamental resonance

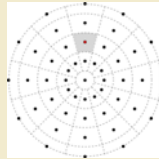
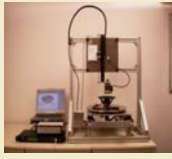
The effective radiation area  $S_D$  is an important lumped parameter describing the surface of a rigid piston moving with the mean value of the voice coil velocity  $v_{coil}$  and generating the same volume velocity  $q$  as the radiator's surface. The integration of the scanned velocity can cope with rocking modes and other asymmetrical vibration profiles.

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# Laser Scanner Technique



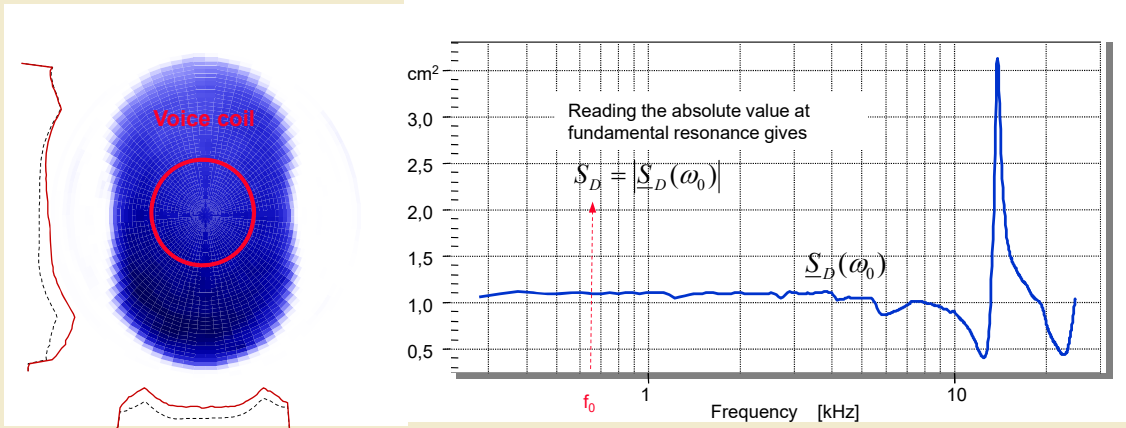
Method:

1. Measurement of vibration and radiator's geometry
2. Integration over surface and voice coil position
3. Calculation of effective radiation area  $S_D(\omega)$
4. Reading  $S_D(\omega_s)$  at fundamental frequency  $\omega_s$

$$\underline{S}_D(\omega) = \frac{\sum \underline{x}(\omega, r_{c,i}) \cdot \Delta S_{c,i}}{\underline{x}_{coil}(\omega)}$$

Problems:

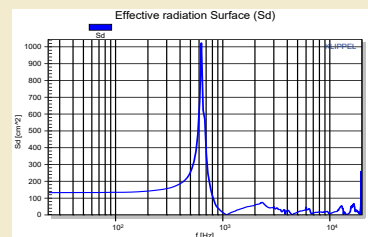
- Surface is covered by grill (surface is not visible for laser)



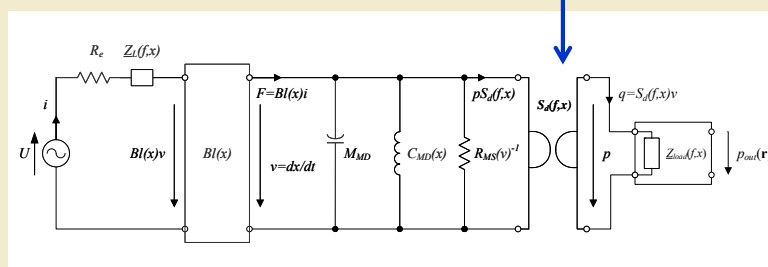
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# Predicting the Acoustical Output at higher frequencies using lumped parameters

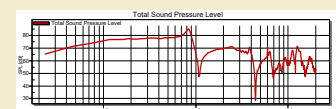


using effective radiation area  $S_D(f)$  as a function of frequency  $f$



useful for transducers having

- high complexity of the mechanical vibration
  - low complexity in radiation directivity ( $ka < 1$ )
- e.g. (in-ear) headphones, microspeaker application

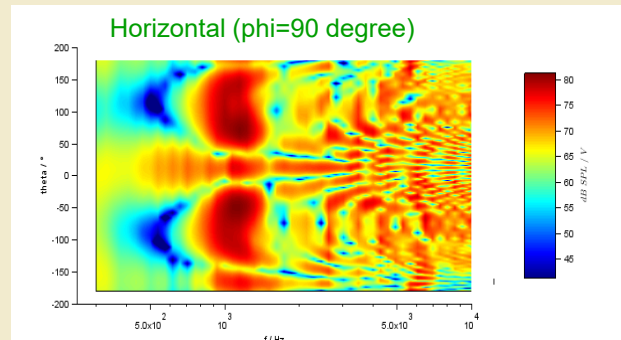
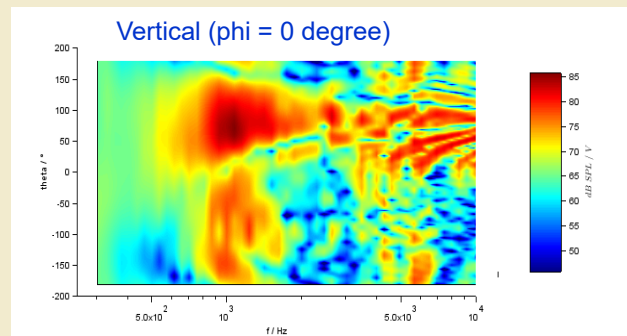
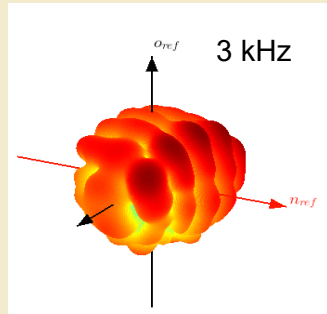
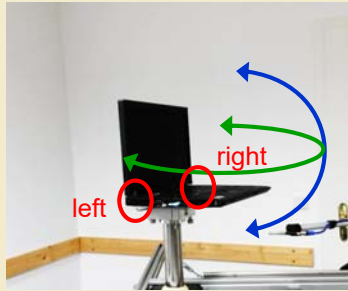


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# Example Microspeaker in Laptop

Far field information

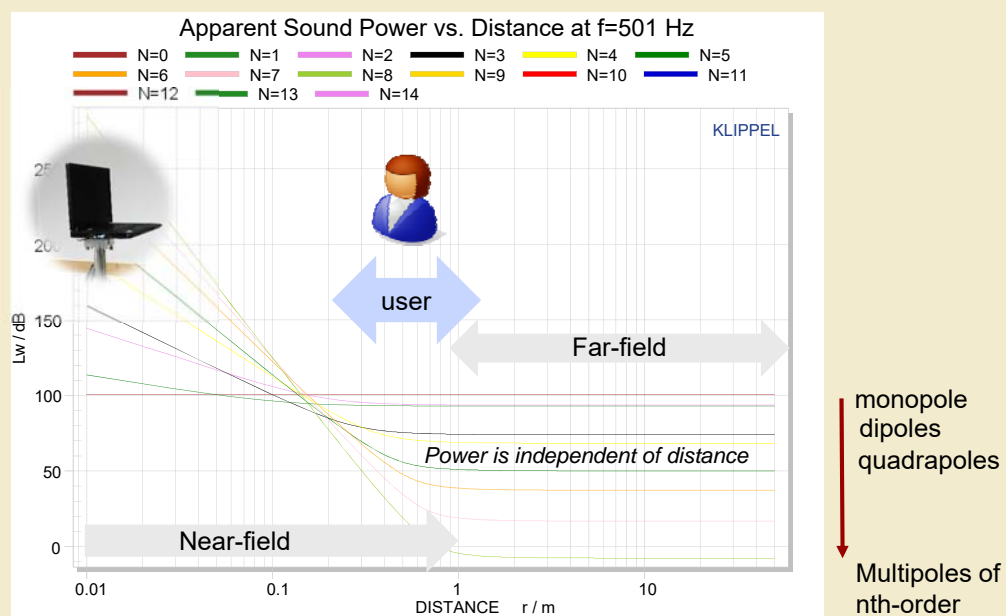


The left and right speaker generate a complex directivity pattern !

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## Is the User Located in the Near-Field or Far-Field?



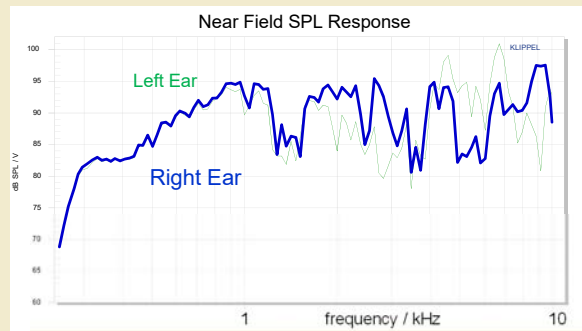
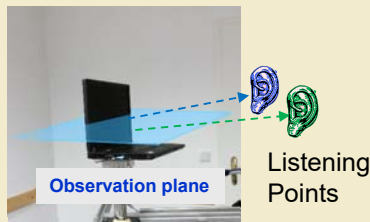
Determining the location of the near and far-fields is important for personal and handheld audio devices !!

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# Comprehensive 3D Information

supports the evaluation of spacial sound effects



SPL distribution



Comprehensive Information

(Amplitude)

(Phase)

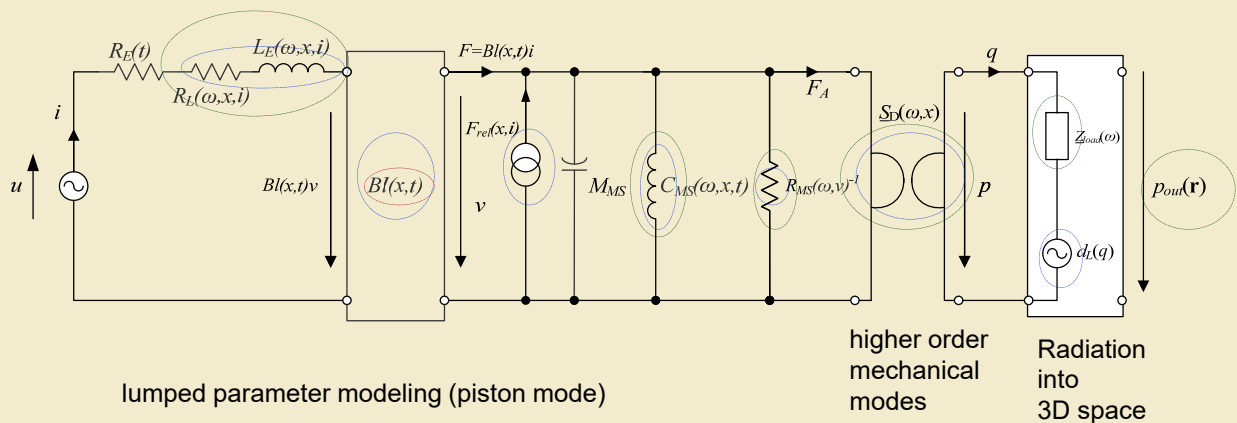
Wave front propagation



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## Transducer Nonlinearities



### Higher-order linear transfer function

- Lossy inductance
- visco elastic creep modeling
- Modal vibration, radiation

### Nonlinearities

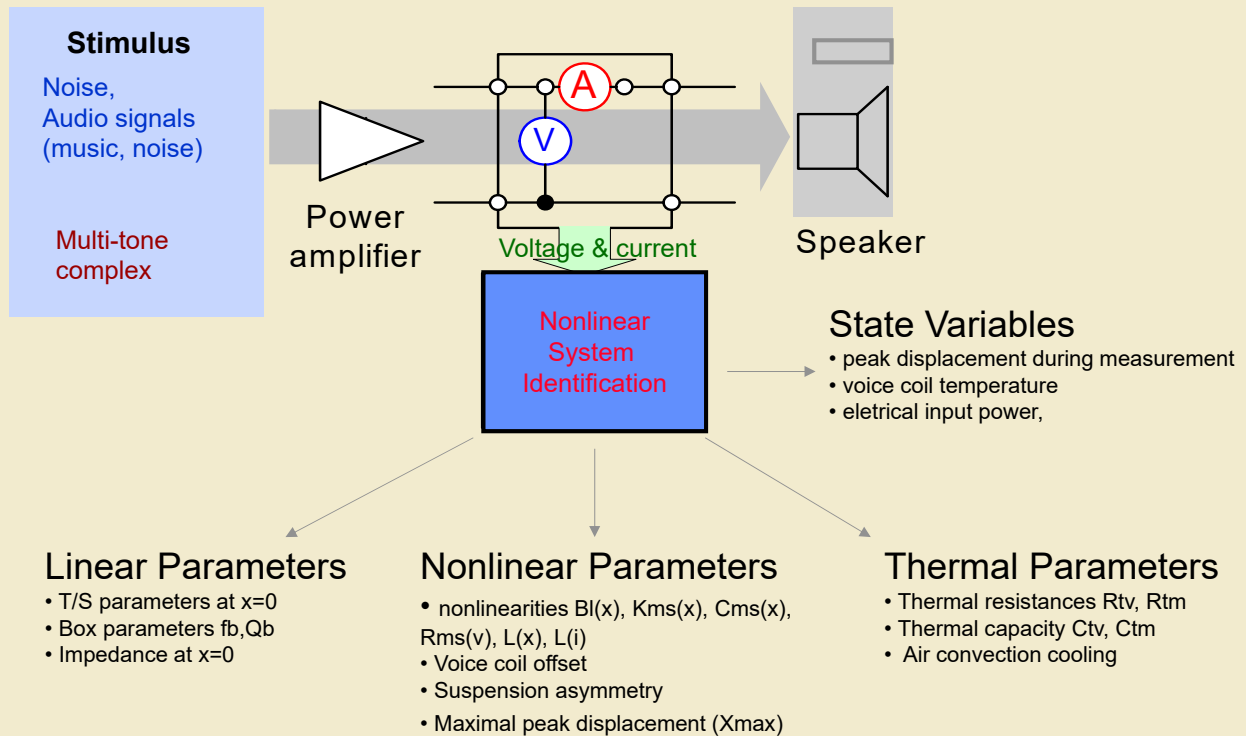
- nonlinear AC flux, reluctance force, inductance
- electro-dynamical motor
- stiffness and damping of suspension
- acoustical system

### Time variant properties

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# Dynamic Measurement of motor and suspension nonlinearities

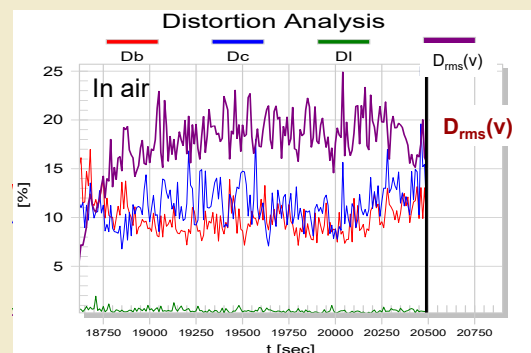
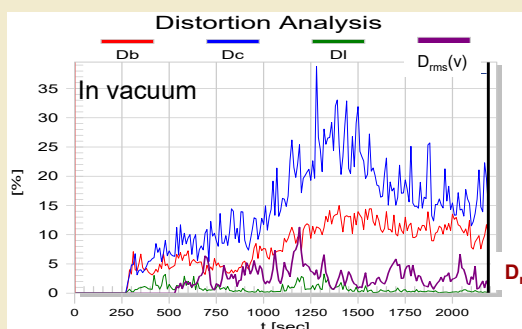
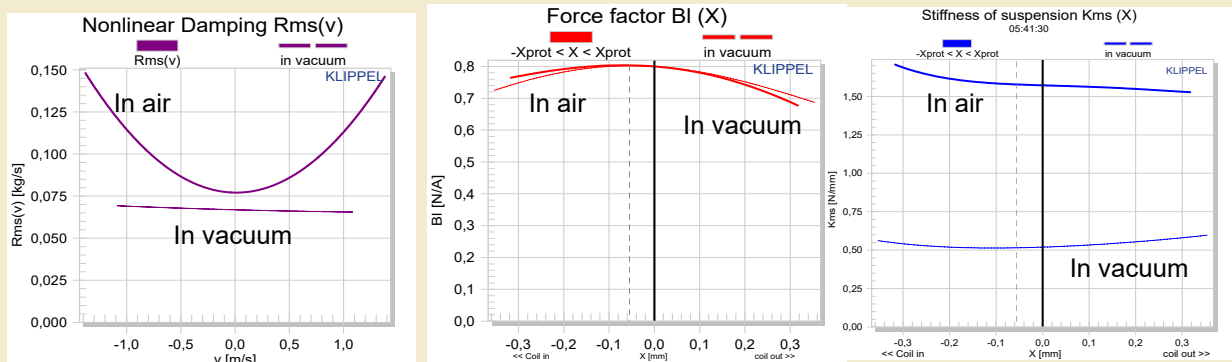


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## Example: Microspeaker

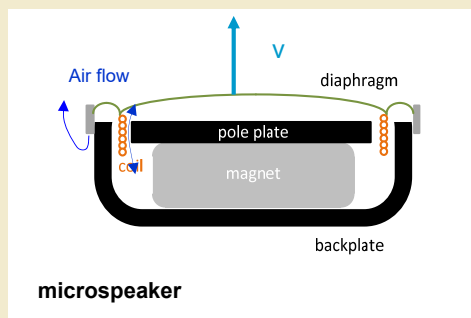
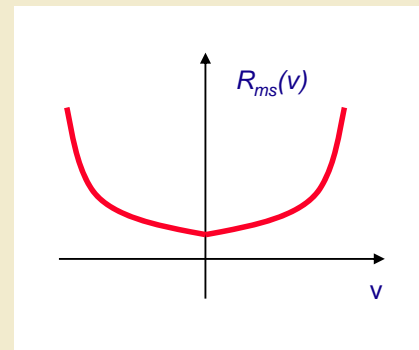
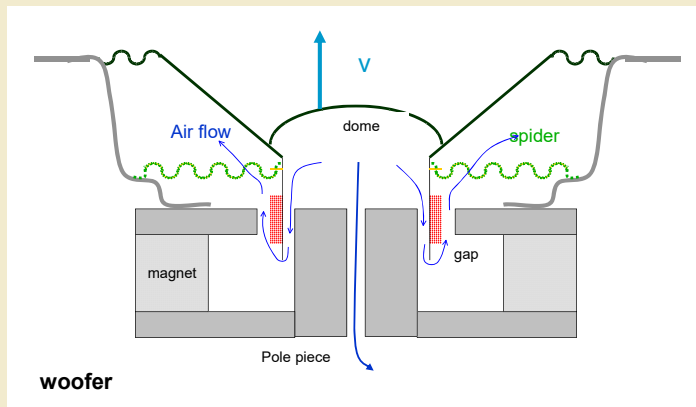
Nonlinear Parameters measured in air and in vacuum



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# Nonlinear Mechanical Resistance $R_{ms}(v)$

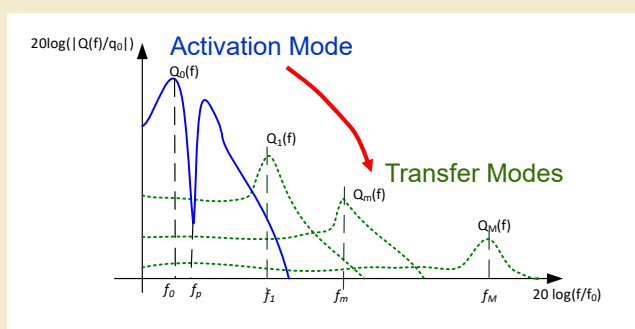
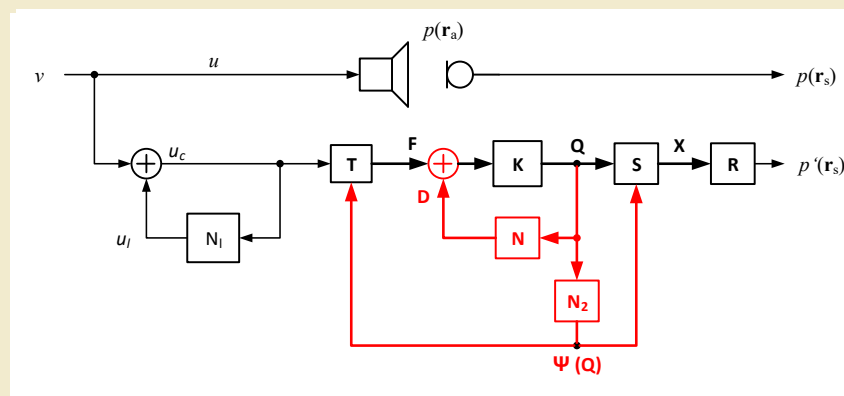


$R_{ms}(v)$  depends on velocity  $v$  of the coil due to air flow and turbulences at vents and porous material (spider, diaphragm)

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## Nonlinear Interactions between Vibration Modes



High amplitudes  $Q$  of the activation mode (e.g. fundamental mode  $Q_0$ ) changes

- Natural frequencies of the transfer modes (higher-order break up modes)
- Mode shape  $\Psi(Q)$  of the transfer mode
- Excitation  $T$  of the transfer modes
- Sound radiation by the transfer modes

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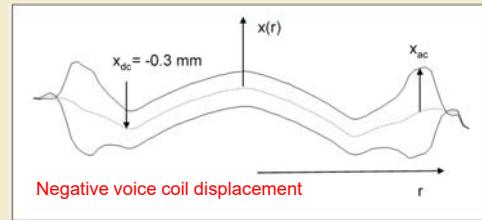
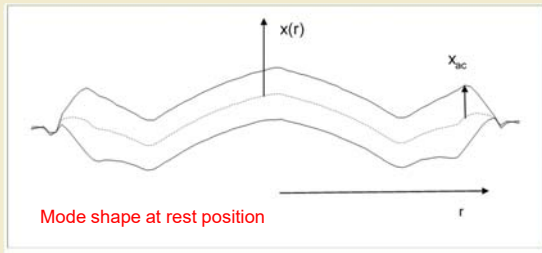




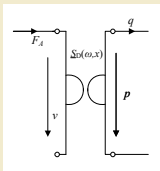
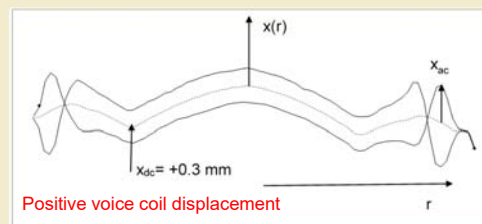
# Nonlinear Variation of the Mode Shape

## Interaction with the fundamental mode

Performing an incremental measurement of the effective radiation area at the original rest position and with a positive and negative offset of 0.3 mm.



The displacement generated by the bass tone generates the geometry of the surround  
→ Other mode shape at higher frequencies



$$\underline{q}(\omega) = \underline{S}_D(\omega, x_{DC})\underline{v}(\omega)$$

$$= \sum_{i=0}^N \underline{S}_i(\omega)\underline{v}(\omega)(x_{DC})^i$$

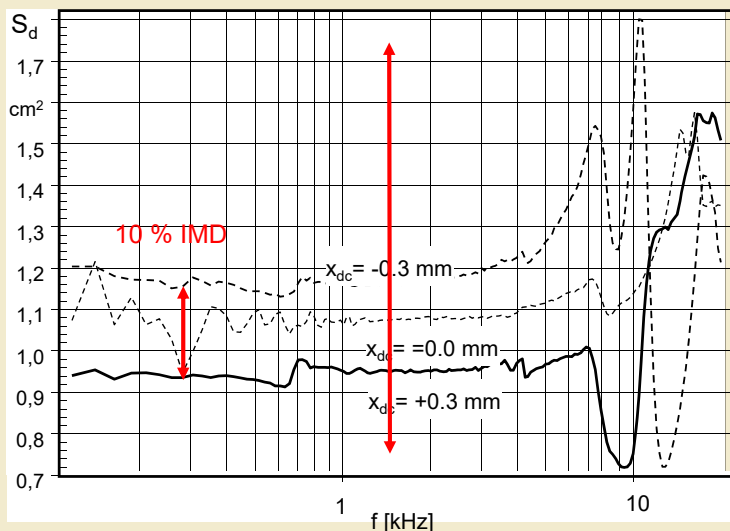
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# Effective Radiation Surface $S_d(f, x)$

## versus frequency $f$ and voice coil displacement $x$

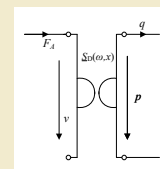
20-50 % IMD



Volume velocity for a DC displacement  $x_{dc}$

$$\underline{q}(\omega) = \underline{S}_D(\omega, x_{DC})\underline{v}(\omega)$$

$$= \sum_{i=0}^N \underline{S}_i(\omega)\underline{v}(\omega)(x_{DC})^i$$



$$q(t) = \sum_{i=0}^N (\mathcal{F}^{-1}\{\underline{S}_i(\omega)\} * v(t))(x(t))^i$$

$$F_A(t) = \sum_{i=0}^N (\mathcal{F}^{-1}\{\underline{S}_i(\omega)\} * q(t))(x(t))^i$$

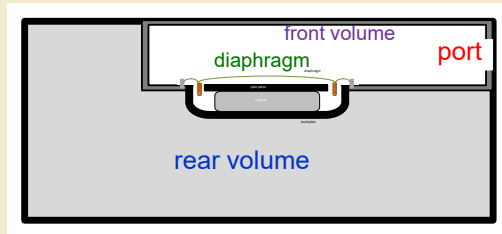
The displacement varying  $S_d(x)$  generates high values of intermodulation distortion

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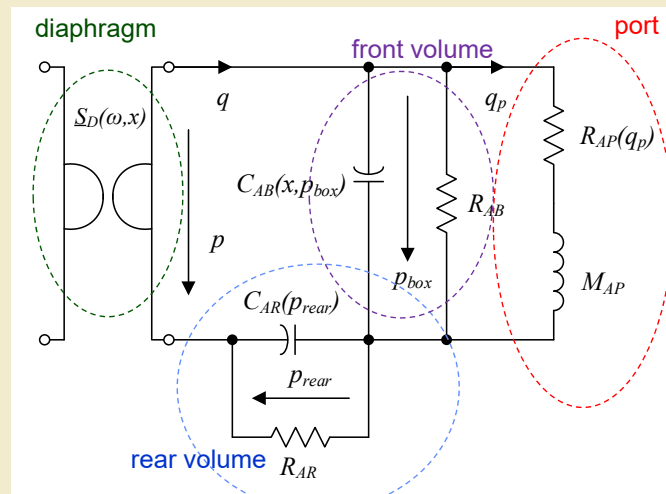


# Modeling of the Acoustic System

Example: Microspeaker mounted in an enclosure with sidefire exit



The voice coil displacement of microspeaker operated in a side fire system is not small compared to the geometrical dimensions of the front volume and rear volume



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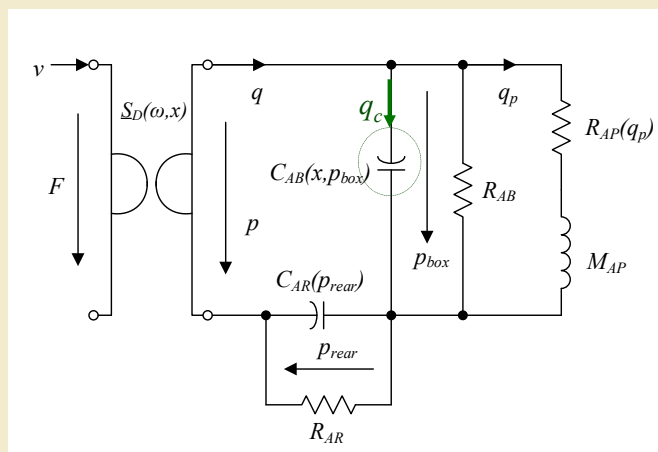


## Dynamic Nonlinear Elements

volume velocity

$$\underline{q}(\omega) = \underline{S}_D(\omega, x) \underline{v}(\omega)$$

$$= \sum_{i=0}^N \underline{S}_i(\omega) \underline{v}(\omega) (x)^i$$



sound pressure at receiving point  $\mathbf{r}$  in the far field

$$p_{out}(\mathbf{r}, t) = \mathbf{F}^{-1} \{ \underline{H}(\mathbf{r}, \omega) \} * q(t) + d_a(\mathbf{r}, t)$$

linear transfer function      nonlinear distortion

Transfer function describing sound radiation and propagation to the point  $\mathbf{r}$  in the far field using Rayleigh equation

$$\underline{H}(\mathbf{r}, \omega) = \frac{j\omega\rho_0}{4\pi S_D(\omega) \underline{v}(\omega)} \int_{S_c} \underline{v}(\omega, \mathbf{r}_c) \frac{e^{-jk|\mathbf{r}-\mathbf{r}_c|}}{|\mathbf{r}-\mathbf{r}_c|} dS_c$$

sound pressure

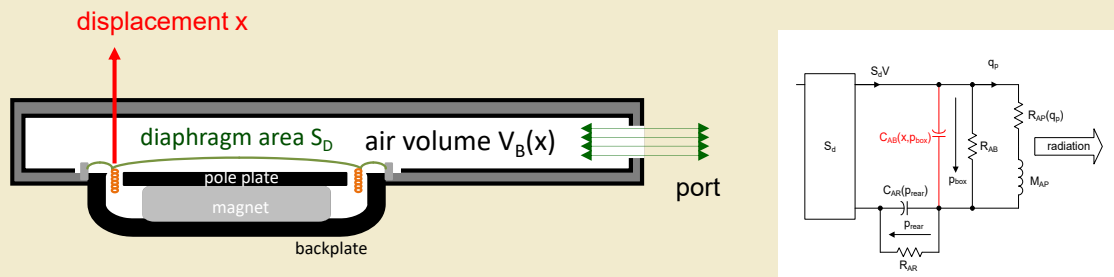
$$p(t) = \mathbf{F}^{-1} \{ \underline{Z}_{load}(\omega) \} * q(t) + d_L(t)$$

acoustical load impedance      nonlinear distortion

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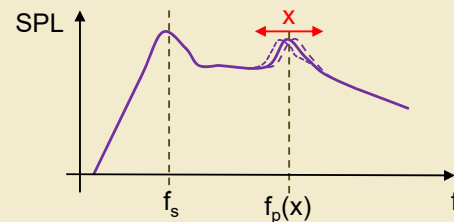
# Air Compliance in Small Vented Enclosures



Compliance  $C_{AB}(x, p)$  of enclosed air

$$C_{AB}(p, x) = \frac{V_0 - S_D x}{\kappa p_0} \left[ 1 - \frac{\kappa + 1}{2\kappa} \left( \frac{p}{p_0} \right) + \frac{\kappa + 1}{6\kappa} \left( 2 + \frac{1}{\kappa} \right) \left( \frac{p}{p_0} \right)^2 \right]$$

with  
static air pressure  $p_0$   
static air volume  $V_0$  at coi's rest position  
adiabatic coefficient  $\kappa$

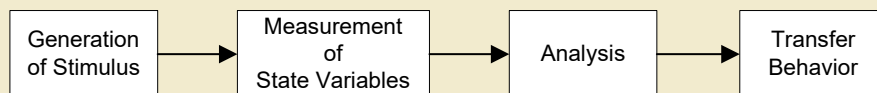


- voice coil displacement  $x$  varies air volume  $V_B(x) = V_0 - S_D x$
- air is not compressed but exchanged with ambience
- Helmholtz resonance  $f_p(x)$  varies with displacement  $x$
- displacement generates intermodulation distortion at port resonance
- critical in small personal audio devices with complex outlet geometry

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## Measurement of Symptoms

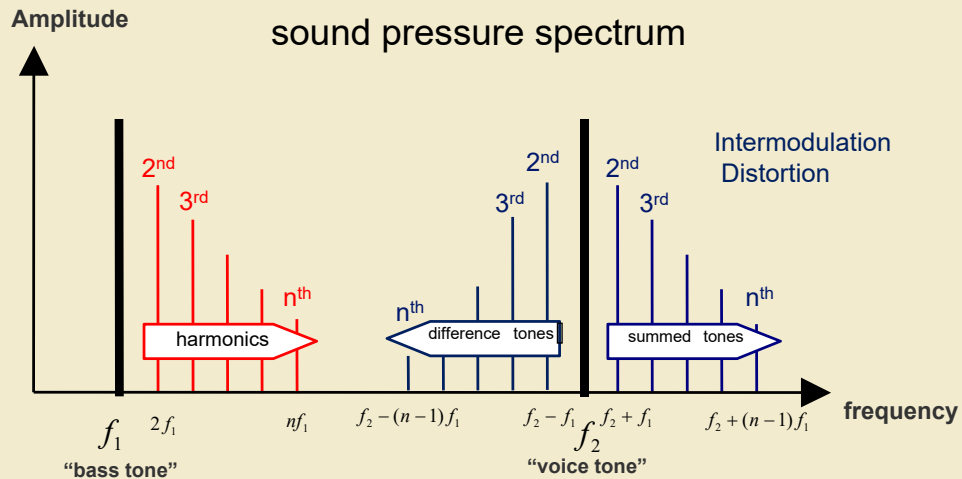
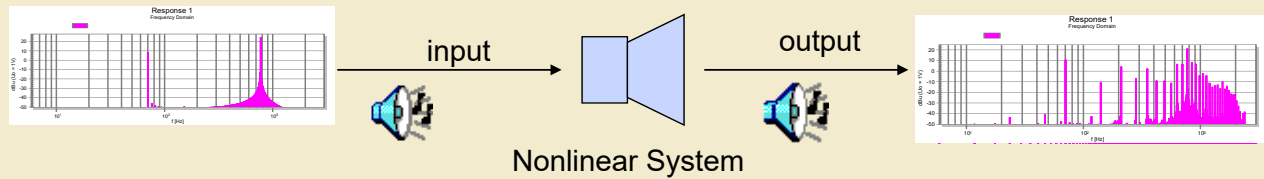


- requires stimulus
- requires special sensor (micro, laser, anemometer)
- applied to selected state variables (pressure, current)
- requires prototype

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# Nonlinear Symptom: New Spectral Components generated by Two-tone Stimulus



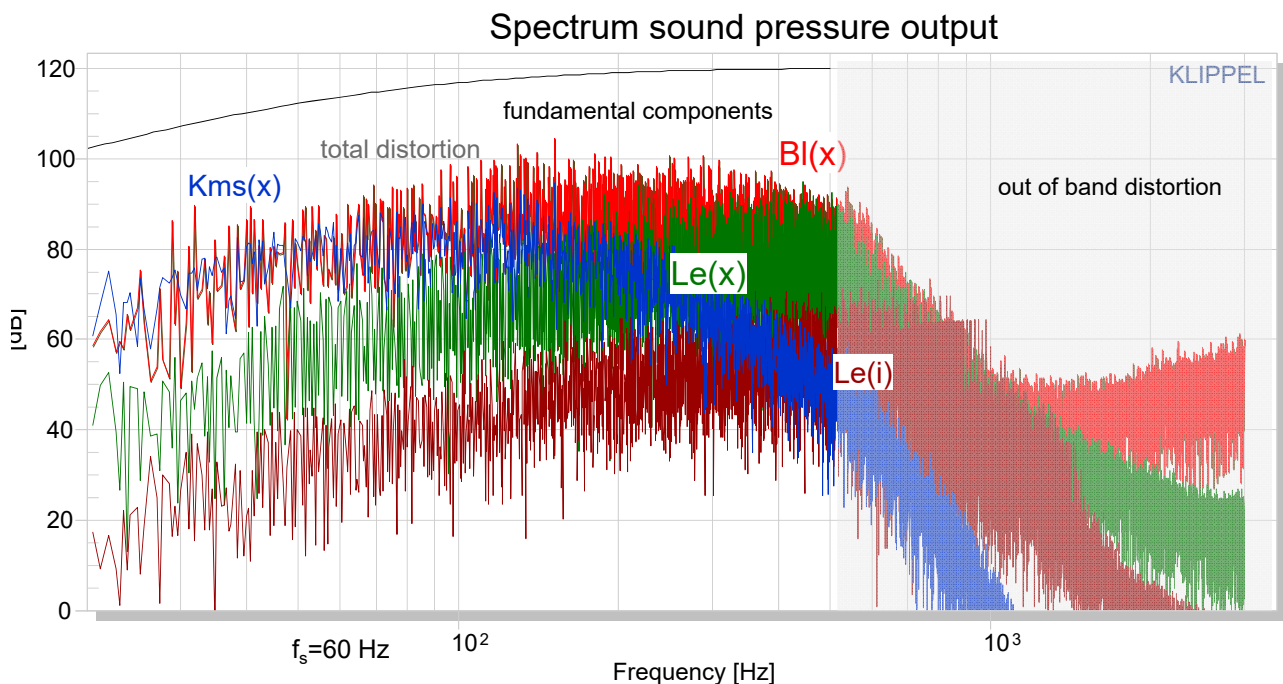
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## Exercise: Woofer

### Analysis of Multi-tone Distortion

causes:  $Le(x)$   $Kms(x)$   $Bl(x)$   $Rms(x,v)$   $Le(i)$  Doppler Effect Cone Vibration

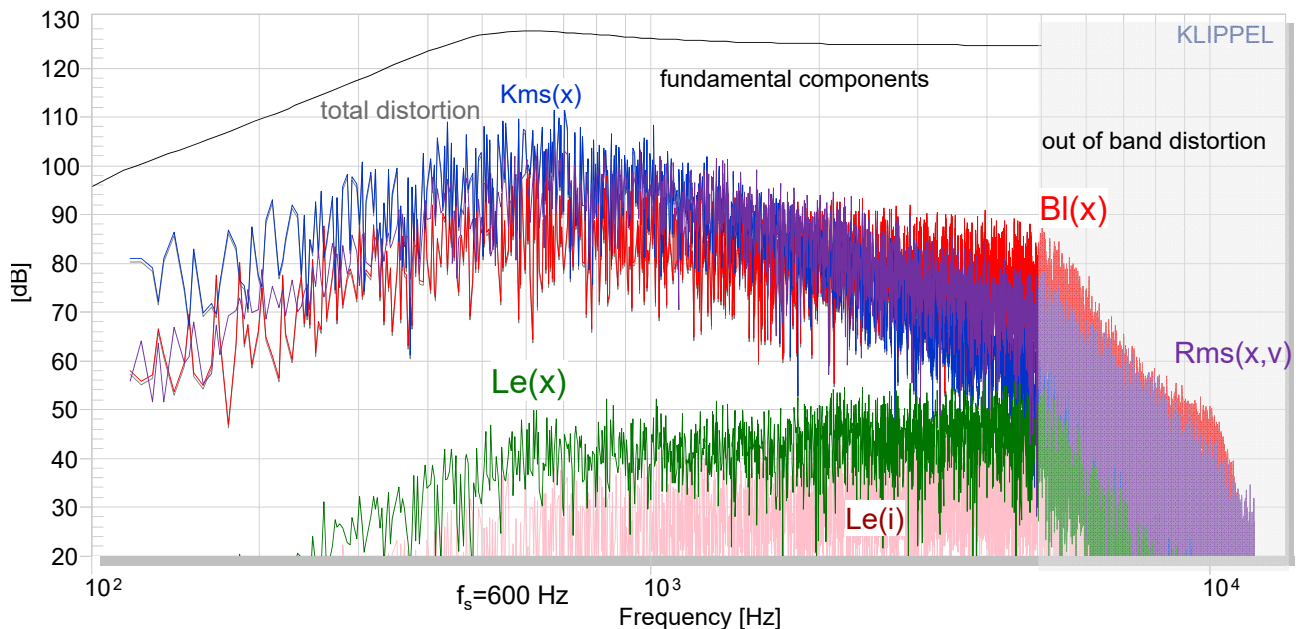


# Exercise: Microspeaker

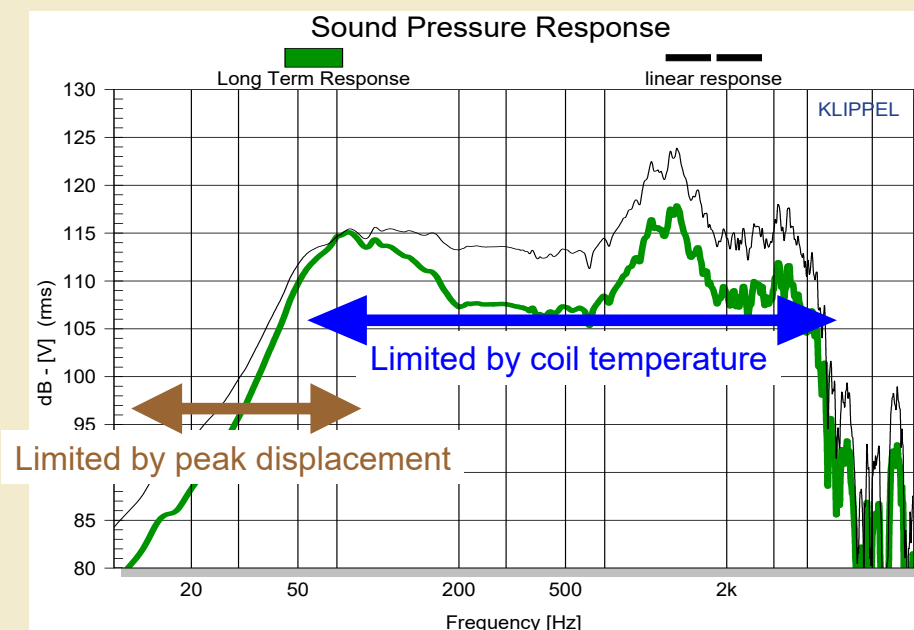
## Analysis of Multi-tone Distortion

causes:  $Le(x)$   $Kms(x)$   $Bl(x)$   $Rms(x,v)$   $Le(i)$  Doppler Effect Cone Vibration

### Distortion Components

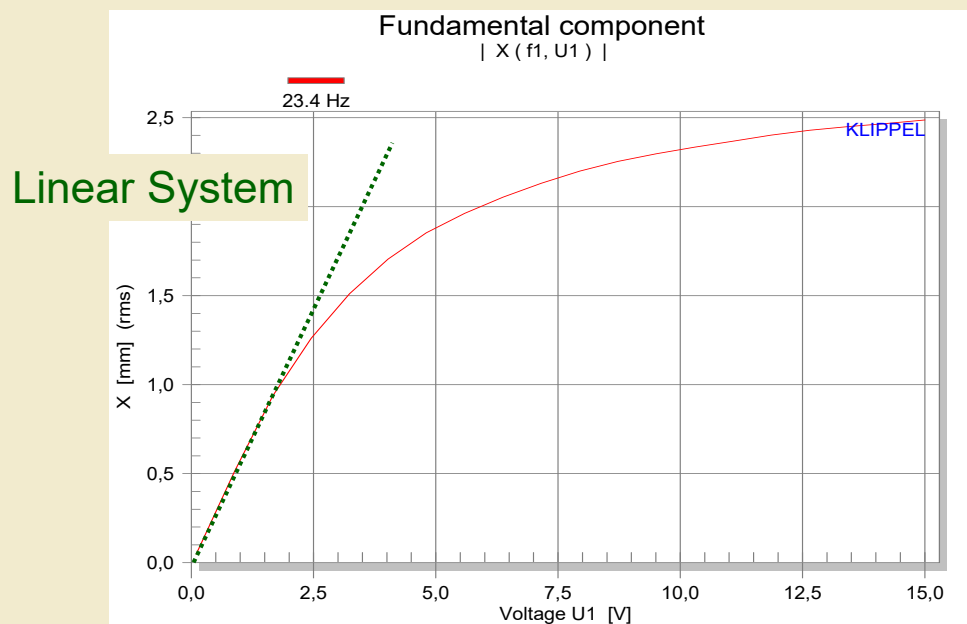


## Compression of SPL Fundamental for a sinusoidal tone versus frequency



Long term response was measured by using a stepped sine wave and cycling 1 min on/1 min off

# Nonlinear Symptom: Amplitude Compression

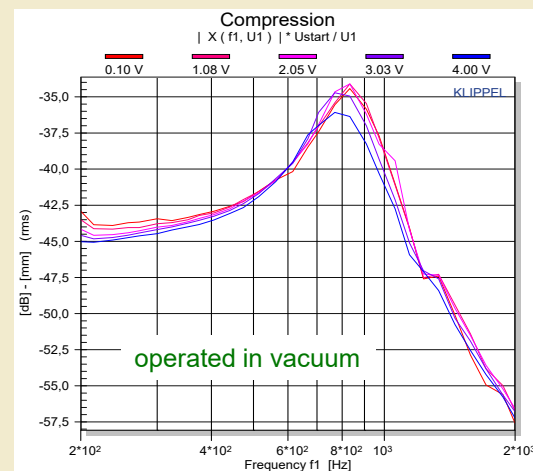
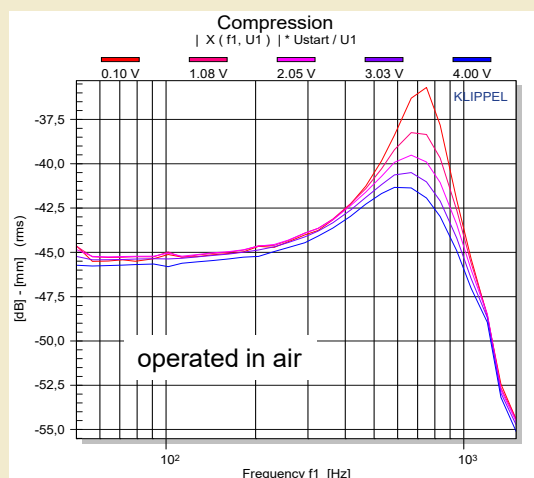


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## Unique Symptom of $R_{ms}(v)$

Compression of the Fundamental Component in a microspeaker



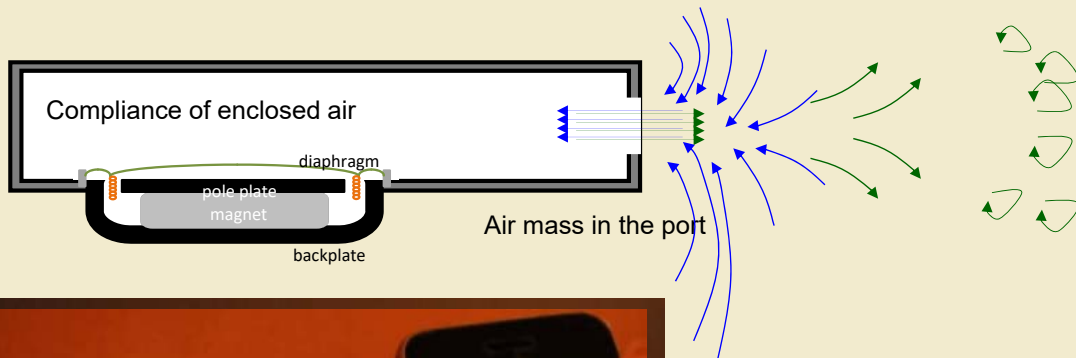
Note: The nonlinear damping caused by  $Bl(x)$  generates the same expansion (more displacement at resonance) in vacuum and in air !!!

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# DC-Air Flow

generated by a smart phone with side-fire port



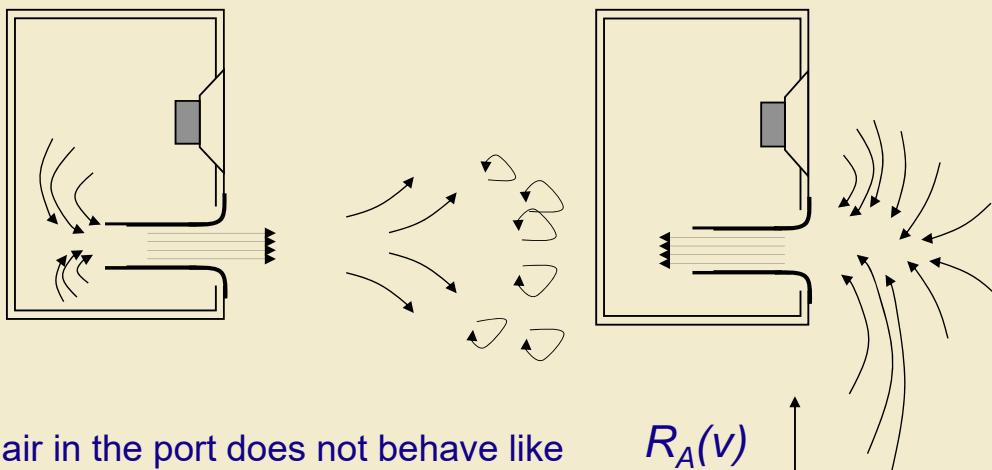
→ Rectification of the AC flow generates jet stream

Courtesy by Qneo see App „Blower“

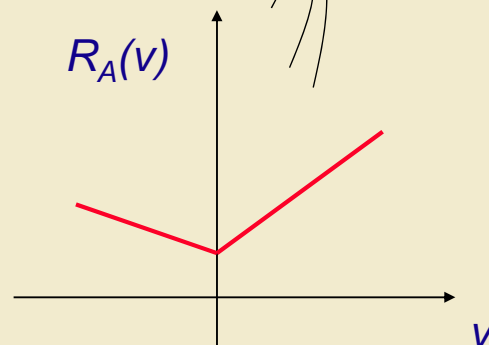
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## Flow Resistance $R_A(v)$ of a Port at Medium Amplitudes



- air in the port does not behave like an air plug
- energy dissipated in the far field
- Harmonics at low frequencies
- $R_A(v) \sim |v| \cdot m$



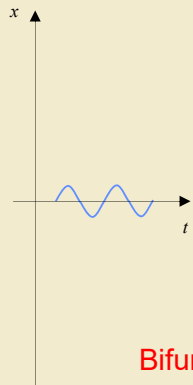
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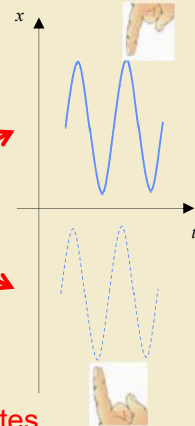


# Nonlinear Symptom: Instability

Small Signal Domain



Large Signal Domain



Bifurcation  
into two states

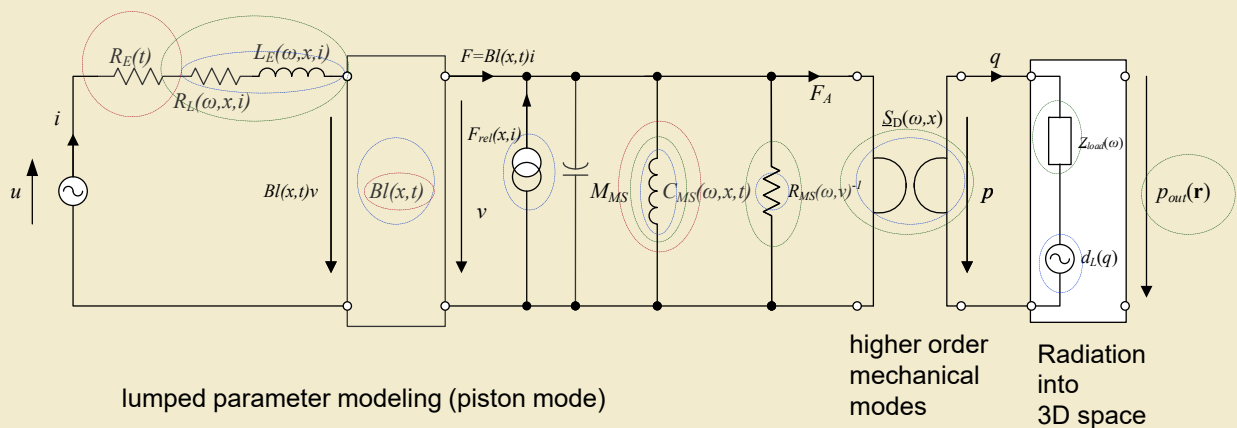


Stimulus: Single tone  
( $f = 1.5\text{fs}$ ) at high  
amplitude

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## Time Variant Properties



### Higher-order linear transfer function

- Lossy inductance
- visco elastic creep modeling
- Modal vibration, radiation

### Nonlinearities

- nonlinear AC flux, reluctance force, inductance
- electro-dynamical motor
- stiffness and damping of suspension
- acoustical system

### Time variant properties

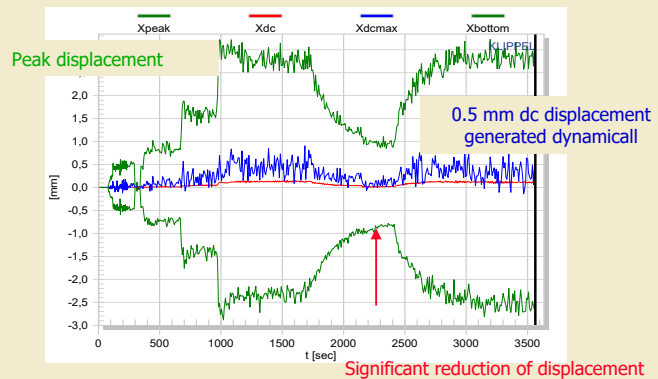
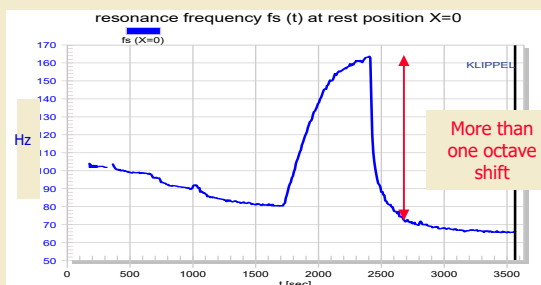
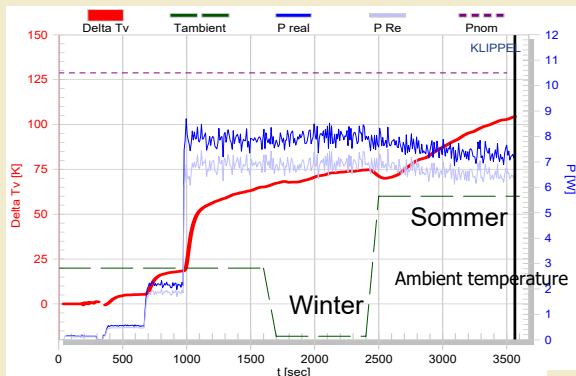
- heating, climate impact, load, fatigue, aging, gravity

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# Influence of Ambient Conditions

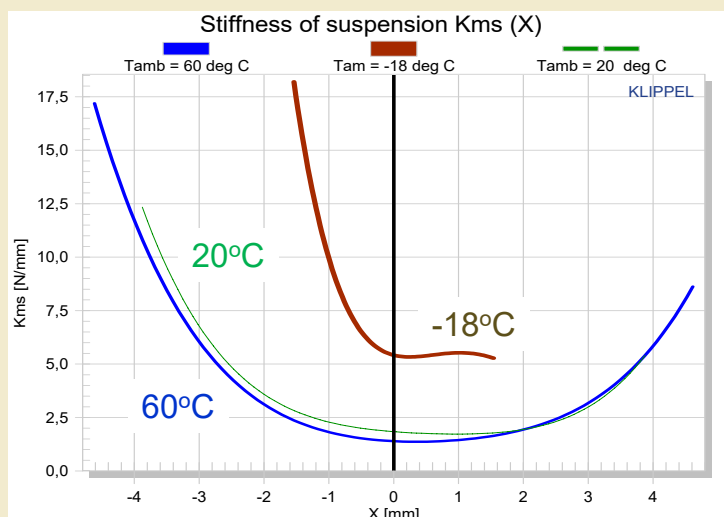
## Environmental Testing



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# Influence of the Climate on Stiffness $K_{ms}(x)$



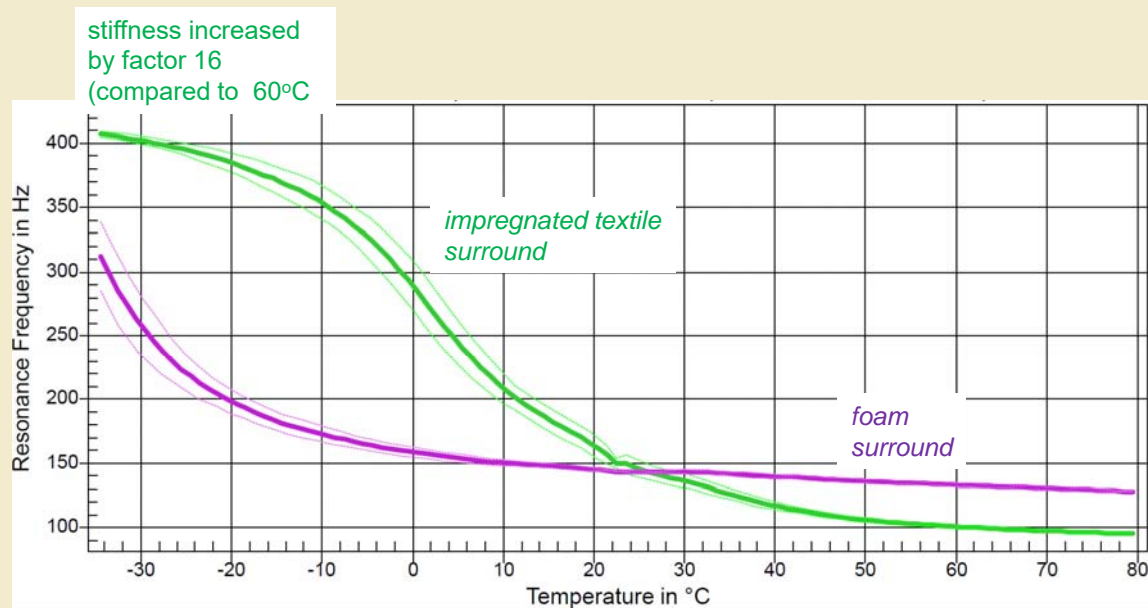
At low ambient temperature (-18 degree C) the rubber surround becomes 4 times stiffer and limits negative peak displacement at -1.5 mm

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# Resonance Frequency versus Ambient Temperature

## two transducers with different surround material



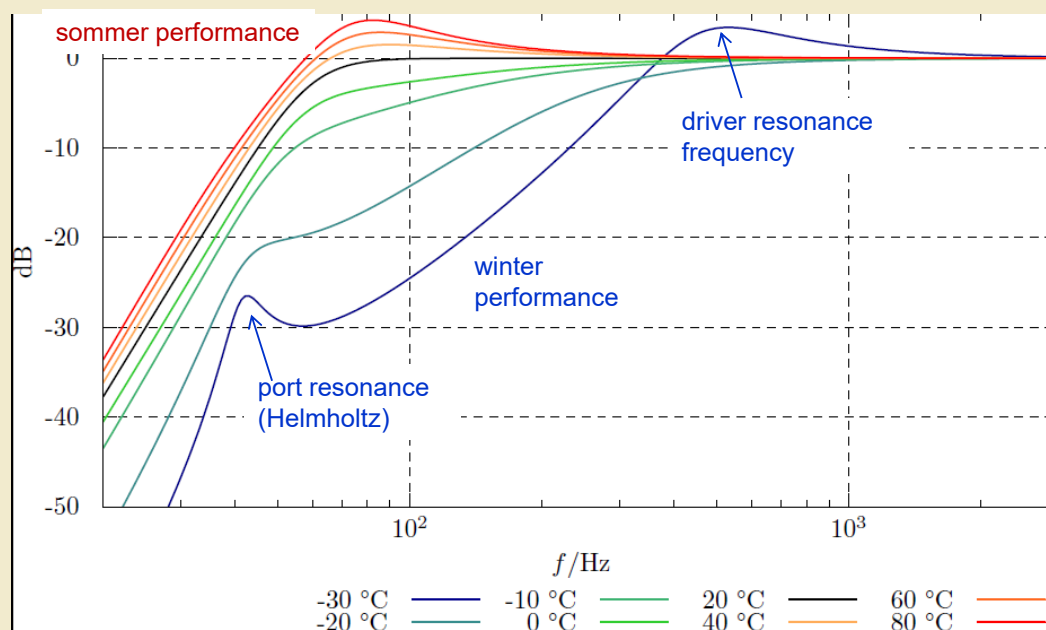
Experiments performed at controlled conditions (30 % relative humidity)  
Details: Diploma Thesis Ch. Kochendörfer TU Dresden, 2011

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# Consequences of Climate Impact

SPL response of a vented loudspeaker system



→ Passive system alignment (box tuning) assumes constant properties of the transducer !!

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# Overview of transducer characteristics

Characteristic	Interpretation	Importance for Micro-speaker	Importance for Headphone	Importance for Loudspeaker
$R_e(t)$	Time variance of the voice coil DC resistance due to thermal dynamics	high	medium	high
$L_e(\omega), R_L(\omega)$	Voice coil inductance and AC resistance depending on frequency	negligible	negligible	high
$L_e(x), R_L(x)$	Voice coil inductance and AC resistance depending on displacement	low	negligible	high
$L_e(i), R_L(i)$	Voice coil inductance and AC resistance depending on current	negligible	negligible	medium
$F_{rel}(x, i)$	Reluctance force depending on voice coil current and displacement x	negligible	negligible	small
$Bl(x)$	Nonlinear force factor depending on displacement x	high	high	high
$Bl(t)$	Time variance of the force factor due an offset in the voice coil rest position	high	high	medium
$C_{MS}(x)$	Nonlinear compliance depending on displacement x	high	high	high
$C_{MS}(t)$	Time variance of the compliance due aging, climate	high	high	high
$C_{MS}(\omega)$ $R_{MS}(\omega)$	Visco-elastic behavior (creep) of the suspension	high	medium	low
$R_{MS}(v)$	Nonlinear mechanical resistance depending on velocity v	high	low	negligible
$v(r_c)-v$	Deviation between distributed voice coil velocity and mean value v	high	high	negligible
RRL	Relative rocking level	high	high	small
$S_D(\omega)$	Frequency dependency of radiation area	low	high	medium
$S_D(x)$	Nonlinear effective radiation area depending on displacement x	high	high	medium
$Z_A(p)$	Nonlinearity of the acoustic Load	high	small	small
$Z_A(\omega)$	Complexity of the frequency dependency of the acoustic load	low	high	low
$H_A(r, \omega)$	Complexity of the directional radiation characteristic	low	low	high
$d_i(q)$	Nonlinear load distortion generated by the acoustical system	high	negligible	medium
$d_A(r, t)$	Nonlinear output distortion generated by the acoustical system	medium	low	low

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## Conclusions

- Microspeakers → major source of innovation
- Innovative transducer design requires more accurate modeling
- Identification of free model parameters → new measurement techniques
- Diagnostics based on parameters becomes more important
- Testing with audio like stimuli required for assessing thermal, nonlinear and time varying properties
- Suspension and radiator is the weakest component !



# Thank you !